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"Procedure for the n value for the Jackson and Hall (1979) correlation"

Procedure nval_jackson (T_PC; T_W; T_F: n_val)

T_PC_K=converttemp(C;K;T_PC)

"Converting

the pseudo-Critical temperature from C to K"

T_W_K=converttemp (C;K;T_W)

"Converting

the wall temperature from C to K"

T_F_K=converttemp (C;K;T_F)

"Converting

the bulk fluid temperature from C to K"

"Conditional statements for calculating the n values to be used in the Jackson and Hall (1979) correlation"

If ((T_F_K<T_W_K) AND (T_W_K<T_PC_K)) OR ((1,2*T_PC_K<T_F_K) AND (T_F_K<T_W_K)) **Then** "Case with nothing accross the PC point"

n_val=0,4

Endif

If ((T_F_K<T_PC_K) AND (T_PC_K<T_W_K)) **Then**

n_val = 0,4+ 0,3* ((T_W_K/T_PC_K)-1)

Endif

If ((T_PC_K<T_F_K) AND (T_F_K< 1,2*T_PC_K)) AND (T_F_K<T_W) **Then**

n_val = 0,4+ 0,2 * ((T_W_K/T_PC_K)-1)* (1-5*((T_W_K/T_PC_K)-1))

Else

n_val=0,4

Endif

End

"Subprogram for Jackson and Hall (1979) correlation"

Subprogram jackson (P_sCO2;G_chan;D_h;T_W;T_F;n_val:Nus_b;Re_b;St)

rho_w= Density (**CarbonDioxide**; T= T_W;P=P_sCO2)

"Density of

the fluid evaluated at the wall temperature"

rho_b=Density (**CarbonDioxide**;T=T_F;P=P_sCO2)

"Density of

the fluid evaluated at the bulk fluid temperature"

h_w= enthalpy(**CarbonDioxide**; T=T_W;P=P_sCO2)

"Enthalpy

of the fluid evaluated at the wall temperature"

h_b=enthalpy(**CarbonDioxide**;T=T_F;P=P_sCO2)

"Enthalpy

of the fluid evaluated at the bulk fluid temperature"

C_p_b=cp(**CarbonDioxide**;T=T_F;P=P_sCO2)

"Specific

heat capacity of the fluid evaluated at the bulk fluid temperature"

T_W_K= converttemp(C;K;T_W)

"Converting

the wall temperature from C to K"

T_F_K=converttemp(C;K;T_F)

"Converting

the bulk fluid temperature from C to K"

c_p_bar= (h_w-h_b)/(T_W_K-T_F_K)

"Integrated

specific heat capacity"

Pr_b=prandtl(**CarbonDioxide**;T=T_F;P=P_sCO2)

"Prandtl

number evaluated at the bulk fluid temperature"

mu_b=viscosity(**CarbonDioxide**;T=T_F;P=P_sCO2)

"Viscosity

evaluated at the bulk fluid temperature"

Re_b= (G_chan*D_h)/mu_b

"Reynolds

number"

Nus_b=0,01831*Re_b^(0,82)*Pr_b^(0,5)* (rho_w/rho_b)^(0,3)* (c_p_bar/C_p_b)^(n_val)

St= Nus_b/Re_b*Pr_b

End

"Procedures for several resistance to be used in the governing equations"

"Procedure for the thermal resistances in the side edge of the bottom portion of the test section"

Procedure r_ech (Th_SE;W_ch;T_int_se1;T_int_ch;L_CV;Th_B;DELTA_seg;R_ax_E_ch)

$\text{DELTA_nodes} = \text{Th_SE}/2 + \text{W_ch}/2$

"Distance

between the node in the edge and the one underneath the flow channel"

$T_{\text{av1}} = \text{average}(T_{\text{int_se1}}; T_{\text{int_ch}})$

"Average of

the temperatures of the nodes in the side edge and the one underneath the flow channel"

$k_1 = \text{conductivity}(\text{Inconel_718}; T = T_{\text{av1}})$

"Thermal

conductivity of the test section material evaluated at the average temperature"

$A_{\text{cross1}} = L_{\text{CV}} * \text{Th_B}$

"Cross

sectional area for conduction"

$R_{\text{ax_E_ch}} = \text{DELTA_nodes} / (k_1 * A_{\text{cross1}})$

"Thermal

resistance to heat transfer from the edge to the location underneath the flow channel"

End

Procedure r_ee (Delta_seg;T_int_se1;T_int_se2;Th_SE;Th_B;R_ax_EE)

$T_{\text{av2}} = \text{average}(T_{\text{int_se1}}; T_{\text{int_se2}})$

"Average of

the temperature of the adjacent nodes inside the side edge of the test section"

$K_2 = \text{conductivity}(\text{Inconel_718}; T = T_{\text{av2}})$

"Thermal

conductivity"

$A_{\text{cross2}} = \text{Th_SE} * \text{Th_B}$

"Cross

sectional area for conduction between adjacent nodes in the side edge"

$R_{\text{ax_EE}} = \text{Delta_seg} / (K_2 * A_{\text{cross2}})$

"Thermal

resistance to heat transfer- axial conduction inside the side edge"

End

"Procedure for the calculation of thermal resistance from the center of the material underneath the flow channel to the wall of the flow channel"

Procedure r_chw (Th_B;T_W;T_int_ch;L_CV;W_ch;R_Ax_ch_w)

$\text{DELTA_res} = \text{Th_B}/2$

"Distance

from the node to the bottom of the flow channel wall"

$T_{\text{av}} = \text{average}(T_{\text{W}}; T_{\text{int_ch}})$

"Average of

the temperatures"

$k = \text{conductivity}(\text{Inconel_718}; T = T_{\text{av}})$

"Thermal

conductivity"

$A_{\text{cross}} = L_{\text{CV}} * W_{\text{ch}}$

"Cross

sectional area for heat transfer"

$R_{\text{Ax_ch_w}} = \text{DELTA_res} / (k * A_{\text{cross}})$

"Thermal

resistance to the flow channel wall"

End

"Procedure for calculation of thermal resistance from the node underneath the flow channel to the one underneath the channel side wall"

Procedure r_chsw (W_ch;Th_SW;T_int_ch;T_int_sw;L_CV;Th_B;R_ax_ch_sw;tau_diff)

$\text{DELTA_res} = (W_{\text{ch}}/2 + \text{Th_SW}/4)$

"Distance

between the nodes"

$T_{\text{Av}} = \text{average}(T_{\text{int_ch}}; T_{\text{int_sw}})$

"Average of

the temperatures"

$k = \text{conductivity}(\text{Inconel_718}; T = T_{\text{Av}})$

"Thermal

conductivity of the bottom portion of the test section"

$A_{\text{cross}} = L_{\text{CV}} * \text{Th_B}$

"Cross

sectional area for heat transfer"

$R_{\text{ax_ch_sw}} = \text{DELTA_res} / (k * A_{\text{cross}})$

"Thermal

resistance"

$\rho = \text{density}(\text{Inconel_718}; T = T_{\text{Av}})$

"Density of

Inconel"

$c = \text{cp}(\text{Inconel_718}; T = T_{\text{Av}})$

"specific

heat capacity"

$\alpha = k / (\rho * c)$

"Thermal

diffusivity"

$\tau_{\text{diff}} = \text{Th_B}^2 / (4 * \alpha)$

"Time for

the thermal wave to reach the outer edge of the wall"

End

"Procedure for calculation of thermal resistance for axial conduction underneath the flow channel"

Procedure r_axch (DELTA_Seg;T_int_ch1;T_int_ch2;Th_B;W_ch;R_ax_ch)

DELTA_res = DELTA_Seg

"Distance

between the nodes"

T_av=**average**(T_int_ch1;T_int_ch2)

"Average of

the temperatures"

k=**conductivity** (Inconel_718;T=T_av)

"Thermal

conductivity of the bottom portion of the test section"

A_cross=Th_B*W_ch

"Cross

sectional area for conduction heat transfer"

R_ax_ch= DELTA_res/(k*A_cross)

"Thermal

resistance for axial conduction underneath the flow channel"

End

"Procedure for axial conduction underneath the channel side walls"

Procedure r_axsw (DELTA_seg;T_int_sw1;T_int_sw2;Th_SW;Th_B;R_ax_sw)

DELTA_res=DELTA_seg

"Distance

between the nodes"

T_av=**average**(T_int_sw1;T_int_sw2)

"Average of

temperatures"

k=**conductivity**(Inconel_718;T=T_av)

"Thermal

conductivity of the bottom portion of the test section"

A_cross=Th_SW*Th_B/2

"Cross

sectional area for thermal conduction"

R_ax_sw= DELTA_res/(k*A_cross)

"Thermal

resistance for axial conduction underneath the channel edge"

End

"Procedure for the convective resistance"

Procedure r_convective (Nus_b;P_sCO2;T_F;D_h;L_CV;W_ch;R_conv;h_conv)

k=**conductivity**(**CarbonDioxide**;T=T_F;P=P_sCO2)

"Thermal

conductivity of the fluid"

h_conv=(Nus_b*k)/D_h

"Heat

transfer coefficient"

A_conv = L_CV*W_ch

"Heat

transfer area for convection"

R_conv= 1/(h_conv*A_conv)

"Convective

resistance"

End

"Procedure for calculating the resistance associated with the conduction dominated region of the boundary layer"

Procedure bl_cond (delta_cl;T_W;L_CV;W_ch;P_sCO2;R_cond_bl)

k_w = **conductivity**(**CarbonDioxide**;T=T_W;P=P_sCO2)

"

Thermal conductivity of the fluid evaluated at the wall temperature"

A_cond = L_CV*W_ch

"Heat

transfer area for conduction"

R_cond_bl = { 200 } delta_cl/(k_w*A_cond)

"

Resistance associated with the conductive portion of the boundary layer"

End

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"Procedure for heat generation inside the bottom portion of the test section"

Procedure heat_gen (N_ch;L_B;T_int_se;T_int_ch;T_int_sw;Th_SE;Th_B;W_ch;Th_SW;L_CV;l_density;q_gen_se;q_gen_ch;q_gen_sw)

T_1= T_int_se

rho_e_se=**electricalresistivity**(Inconel_718;T=T_1)

"Electrical

resistivity in the side edge - bonding region"

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rho_e_ch=electricalresistivity(Inconel_718; T=T_int_ch)
Electrical resistivity underneath the flow channel"
rho_e_sw=electricalresistivity(Inconel_718; T=T_int_sw)
Electrical resistivity in the channel side wall"
A_cross_se=Th_SE*Th_B
sectional area for current flow in the side edge"
A_cross_ch= W_ch*Th_B
sectional area for current flow underneath the flow channel"
A_cross_sw= (Th_SW/2)*Th_B
sectional area for the current flow in the side wall"
R_se=(L_CV*rho_e_se)/A_cross_se
resistance in the side edge of the test section"
R_ch=(L_CV*rho_e_ch)/A_cross_ch
resistance underneath the flow channel"
R_sw=(L_CV*rho_e_sw)/A_cross_sw
resistance in the side wall"
q_gen_se= (I_density*A_cross_se)^2*R_se
generation inside the side edge"
q_gen_ch=(I_density*A_cross_ch)^2*R_ch
generation under the flow channel"
q_gen_sw=(I_density*A_cross_sw)^2*R_sw
generation in the channel side wall"

W_total = (2*Th_SE)+(N_ch-1)*(Th_SW)+N_ch*W_ch
of the test section"
A_cross_total = W_total*Th_B
sectional area for current flow"
R_total= (rho_e_ch*L_B)/A_cross_total
End

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"Procedure for evaluating the buoyancy threshold criterion proposed by Petukhov and flow acceleration effects according to Jackson's criterion"

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Procedure grashof (T_W;T_F;D_h;P_sCO2;q_flux;G_chan;Re_b;per;per_heated:Bo_pet;Psi_Jackson;K_v)
T_av=average(T_W;T_F)
temperature- average of the wall temperature and the bulk fluid temperature"
rho_b= density(CarbonDioxide;T=T_F;P=P_sCO2)
carbon dioxide evaluated at the bulk fluid temperature"
rho_w=density(CarbonDioxide;T=T_W;P=P_sCO2)
carbon dioxide evaluated at the channel wall temperature"
rho_film=density(CarbonDioxide;T=T_av;P=P_sCO2)
carbon dioxide evaluated at the film temperature"
mu_b=viscosity(CarbonDioxide;T=T_F;P=P_sCO2)
of carbon dioxide evaluated at the bulk fluid temperature"
nu_b=kinematicviscosity(CarbonDioxide;T=T_F;P=P_sCO2)
viscosity of carbon dioxide evaluated at the bulk fluid temperature"
h_w=enthalpy(CarbonDioxide;T=T_W;P=P_sCO2)
of carbon dioxide evaluated at the channel wall temperature"
h_b=enthalpy(CarbonDioxide; T=T_F;P=P_sCO2)
of carbon dioxide evaluated at the bulk fluid temperature"
k_b=conductivity(CarbonDioxide; T=T_F;P=P_sCO2)
Conductivity of carbon dioxide evaluated at the bulk fluid temperature"
Pr_bar = (h_w-h_b)/(T_W-T_F) * (mu_b/k_b)
Prandtl number"
Beta_bar= 1/(rho_film)* ((rho_b-rho_w)/(T_W-T_F))
Gr_q= (g#*Beta_bar*q_flux*D_h^4)/(nu_b^2*k_b)
Gr_th=3*10^(-5)*Re_b^(2,75)*Pr_bar^(0,5)*(1+2,4*Re_b^(-1/8)*(Pr_bar^(2/3)-1))
Bo_pet = Gr_q/Gr_th
"

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"Jackson's flow acceleration"

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Beta_b=volexpcoef(CarbonDioxide;T=T_F;P=P_sCO2)
Volume expansion coefficient for carbon dioxide evaluated at the bulk fluid temperature"
Pr_b=Prandtl (CarbonDioxide;T=T_F;P=P_sCO2)
number for carbon dioxide evaluated at the bulk fluid temperature"
mu_film=viscosity(CarbonDioxide;T=T_av;P=P_sCO2)
of carbon dioxide evaluated at the film temperature"
F_VP1= (mu_film/mu_b)*(rho_film/rho_b)^(-0,5)
property function"

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A_cb = (Beta_b*q_flux*D_h)/(k_b*Re_b^(1,625)*Pr_b)
Acceleration function"
C_A= 10^4
Psi_Jackson= C_A*A_cb*F_VP1
accelration parameter"

"Jackson acceleration parameter applied to asymmetric heating"
cp_b=cp(CarbonDioxide;T=T_F;P=P_sCO2)
heat capacity for carbon dioxide evaluated at the bulk fluid temperature"

q_plus = Beta_b*q_flux/(G_chan*cp_b);
K_v = 4*(per_heated/per)*q_plus/Re_b;
End

"Procedure for evaluating the bulk fluid velocity in the channel"
Procedure velocity (N_ch;W_ch;H_ch;D_h;AR;m_dot_total;T_F;T_W;P_sCO2;L_ax;V_channel;nu_acc;span_spacing;
y_plus;Re_chan;F_channel;dp_dx;dp;rho_bulk;DELTA_Bankston;DELTA_P_W;tau_near_wall;u_friction;rho_wall;delta_cl)
A_chan= W_ch*H_ch
of a single channel"
m_dot_chan= m_dot_total/N_ch
rate through a single channel"
G_chan= m_dot_chan/A_chan
through a single channel"
rho_bulk= density(CarbonDioxide;T=T_F;P=P_sCO2)
the fluid evaluated at the bulk fluid temperature"
rho_wall= density(CarbonDioxide;T=T_W;P=P_sCO2)
the fluid evaluated at the wall temperature"
mu_wall=viscosity(CarbonDioxide; P=P_sCO2;T=T_W)
Viscosity of the fluid evaluated at the wall temperature"
V_channel= G_chan/rho_bulk
velocity in the channel"
nu_acc=kinematicviscosity(CarbonDioxide;T=T_W;P=P_sCO2)
viscosity evaluated at the wall temperature"
RR= AR/D_h
roughness for the flow channel"
mu_b=viscosity(CarbonDioxide;T=T_F;P=P_sCO2)
evaluated at the bulk fluid temperature"
Re_chan= (G_chan*D_h)/mu_b
number in the channel"
Theta_1_pipe=(2,457*ln(((7/Re_chan)**0,9+0,27*RR)**(-1)))**16
Theta_2_pipe=(37530/Re_chan)**16
F_channel=8*((8/Re_chan)**(12)+(Theta_1_pipe+Theta_2_pipe)**(-1,5))**(1/12)
friction factor for turbulent flow in channels"
tau_s= (rho_wall*F_channel*V_channel^2)/8
dp_dx= (F_channel*rho_bulk*V_channel^2)/(2*D_h)
drop/length"
dp=dp_dx*L_ax
f_flowacc= 0,079*Re_chan^(-0,25)
tau_wall= (rho_bulk*V_channel^2)*f_flowacc/2
u_friction=sqrt(tau_wall/rho_bulk)
velocity"
Span_spacing_ND = 100
dimensional span wise spacing of coherent structures"
span_spacing= (Span_spacing_ND*nu_acc)/u_friction
y_star= nu_acc/u_friction
length scale"
y_plus=H_ch/y_star
delta_vs_plus = 5 [-]
Dimensionless thickness of the viscous sub-layer"
Pr_w = prandtl(CarbonDioxide;T=T_W;P=P_sCO2)
number evaluated at the wall temperature"
delta_cl_plus = delta_vs_plus/(Pr_w^(1/3))
Dimensionless thickness of the conduction dominated region of the boundary layer"
delta_cl = delta_cl_plus*y_star
Dimensional thickness of the conduction dominated region of the boundary layer"
DELTA_Bankston = (nu_acc/(rho_wall*u_friction^3))*dp_dx

DELTA_P_W= (-4*mu_wall/D_h)* (1/sqrt(rho_wall*tau_s))

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tau_near_wall=rho_wall*u_friction^2
C_f= 0,0376*(Re_chan)^(-1/6)
friction coefficient as defined in Patel and Head 1968"
DELTA_patel= -nu_acc/(rho_wall*u_friction^3)*dp_dx
End

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"Skin

"Procedure implementing Wien's law of radiation"

Procedure wien (T_BW:Lambda_max;F_rad)

C_rad= 2897,8

T=**converttemp**(C;K; T_BW)

Lambda_max=C_rad/T

Lambda_1= 7,5

Lambda_2 = 13

F_rad=**blackbody**(T;Lambda_1;Lambda_2)

End

"-----"

"Dimensions of the bottom portion of the test section"

Th_B=254***convert**(micron;m)

"Thickness

of the bottom Inconel 718sheet"

L_B= 50***convert**(mm;m)

"Length of

the bottom Inconel 718 sheet"

W_ch= 1,92***convert**(mm;m)

"Width of

the flow channel"

Th_SW=1,5***convert**(mm;m)

"Width of

the wall seperating the channels"

Th_SE=1,5***convert**(mm;m)

"Width of

the side edge used for bonding the Inconel 718 to Macor"

AR= 0,78***convert**(micron;m)

"Absolute

roughness of the channel walls"

"Flow channel hydraulic diameter"

H_ch= 600***convert**(micron;m)

"Height of

the flow channels"

A_cross_flow = H_ch*W_ch

"Flow cross

sectional area"

per= 2*(H_ch+W_ch)

"Perimeter"

per_heated = W_ch

"Heated

perimeter"

D_h= (4*A_cross_flow)/per

"Hydraulic

diamter"

"Flow conditions"

P_sCO2_psi= 1120 [psi]

"Absolute

pressure in the test section in psi"

P_sCO2 =P_sCO2_psi***convert**(psi;kPa)

"Absolute

pressure in the test section in kPa"

P_sCO2_bar= P_sCO2_psi***convert**(psi;bar)

"Absolute

pressure in the test section in bar"

G_chan = 500 [kg/m^2-s]

"Mass flux

in a single channel"

m_dot_chan= G_chan*A_cross_flow

"Mass flow

rate in a single channel"

m_dot_total=m_dot_chan*N_ch

"Total mass

flow rate through the test section"

G_total=G_chan

N_ch=3

T_F_in = 32,5 [C]

"Inlet

temperature"

"Defining the pseudo-critical temperature"

T_PC= -122,6+6,124*P_sCO2_bar-0,1657*P_sCO2_bar^2+0,01773*P_sCO2_bar^(2,5)-0,0005608*P_sCO2_bar^3 "

Pseudo-critical temperature - Liao and Zhao (2002)"

"Current"

I_curr=55[Amp]

"Current

through the test section"

$W_{total} = (2*Th_{SE}) + (N_{ch}-1)*Th_{SW} + N_{ch}*W_{ch}$
of the test section"

"Total width

$A_{cross_total} = W_{total}*Th_B$
sectional area for current flow"

"Total cross

$I_{density} = I_{curr}/A_{cross_total}$

"Segmenting the model in the third dimension"

$N_{nodes} = 40[-]$

"Number of

nodes in the bottom portion of the test section"

$L_{begin} = 0 [m]$

"Left edge

of the test section"

$DELTA_{seg} = L_B / (N_{nodes}-1)$

"Distance

between the nodes"

"Assigning the position to the nodes"

Duplicate i= 1;N_nodes

$L_{ax}[i] = L_{begin} + DELTA_{seg} * (i-1)$

End

"Assigning the length to the control volumes"

$L_{CV}[1] = DELTA_{seg}/2$

"Length of

the first control volume"

$L_{CV}[N_{nodes}] = L_{CV}[1]$

"Length of

the last control volume"

"Length of the control volumes in the internal control volumes"

Duplicate i=2;(N_nodes-1)

$L_{CV}[i] = DELTA_{seg}$

End

"Calling all the procedures here"

Duplicate i=1;N_nodes

Call nval_jackson (T_PC; T_W[i];T_F[i]; n_val[i])

Call jackson (P_sCO2;G_chan;D_h;T_W[i];T_F[i];n_val[i];Nus_b[i];Re_b[i];St[i])

{Nus_b[i] = 20}

Call r_chw (Th_B;T_W[i];T_int_ch[i];L_CV[i];W_ch;R_Ax_ch_w[i])

Call r_chsw (W_ch;Th_SW;T_int_ch[i];T_int_sw[i];L_CV[i];Th_B;R_ax_ch_sw[i];tau_diff[i])

Call r_convective (Nus_b[i];P_sCO2;T_F[i];D_h;L_CV[i];W_ch;R_conv[i];h_conv[i])

Call bl_cond (delta_cl[i];T_W[i];L_CV[i];W_ch;P_sCO2;R_cond_bl[i])

Call heat_gen (N_ch;L_B;T_int_se[i];T_int_ch[i];T_int_sw[i];Th_SE;Th_B;W_ch;Th_SW;L_CV[i];I_density;q_gen_se[i];
q_gen_ch[i];q_gen_sw[i])

Call r_ech (Th_SE;W_ch;T_int_se[i];T_int_ch[i];L_CV[i];Th_B;DELTA_seg;R_ax_E_ch[i])

Call grashof (T_W[i];T_F[i];D_h;P_sCO2;q_flux[i];G_chan;Re_b[i];per;per_heated;Bo_pet[i];Psi_Jackson[i];K_v[i])

Call velocity (N_ch;W_ch;H_ch;D_h;AR;m_dot_total;T_F[i];T_W[i];P_sCO2;L_ax[i];V_channel[i];nu_acc[i];span_spacing[i];
y_plus[i];Re_chan[i];F_channel[i];dp_dx[i];dp[i];rho_bulk[i];DELTA_Bankston[i];DELTA_P_W[i];tau_near_wall[i];u_friction[i];
rho_wall[i];delta_cl[i])

Call wien (T_int_ch[i];Lambda_max[i];F_rad[i])

End

Duplicate i=1;(N_nodes-1)

Call r_axch (DELTA_Seg;T_int_ch[i];T_int_ch[i+1];Th_B;W_ch;R_ax_ch[i])

Call r_axsw (DELTA_seg;T_int_sw[i];T_int_sw[i+1];Th_SW;Th_B;R_ax_sw[i])

Call r_ee (DELTA_seg;T_int_se[i];T_int_se[i+1];Th_SE;Th_B;R_ax_EE[i])

End

"-----"

"Governing equations"

"Energy balance for the nodes at the edge"

"The first node"

$$q_{\text{gen_se}}[1] = (T_{\text{int_se}}[1] - T_{\text{int_ch}}[1]) / R_{\text{ax_E_ch}}[1] + (T_{\text{int_SE}}[1] - T_{\text{int_SE}}[2]) / R_{\text{ax_EE}}[1]$$

$$(T_{\text{int_se}}[1] - T_{\text{int_ch}}[1]) / R_{\text{ax_E_ch}}[1] + q_{\text{gen_ch}}[1] = (T_{\text{int_ch}}[1] - T_{\text{W}}[1]) / R_{\text{ax_ch_w}}[1] + (T_{\text{int_ch}}[1] - T_{\text{int_ch}}[2]) / R_{\text{ax_ch}}[1] + (T_{\text{int_ch}}[1] - T_{\text{int_sw}}[1]) / R_{\text{Ax_ch_sw}}[1]$$

$$q_{\text{gen_sw}}[1] + (T_{\text{int_ch}}[1] - T_{\text{int_sw}}[1]) / R_{\text{Ax_ch_sw}}[1] = (T_{\text{int_sw}}[1] - T_{\text{int_sw}}[2]) / R_{\text{ax_sw}}[1]$$

$$(T_{\text{int_ch}}[1] - T_{\text{W}}[1]) / R_{\text{ax_ch_w}}[1] = (T_{\text{W}}[1] - T_{\text{F}}[1]) / R_{\text{conv}}[1]$$

$$q_{\text{conv}}[1] = (T_{\text{W}}[1] - T_{\text{F}}[1]) / R_{\text{conv}}[1]$$

$$m_{\text{dot_chan}} * h_{\text{in}} + (T_{\text{W}}[1] - T_{\text{F}}[1]) / R_{\text{conv}}[1] = m_{\text{dot_chan}} * h[1]$$

$$h_{\text{in}} = \text{enthalpy}(\text{CarbonDioxide}; P = P_{\text{sCO2}}; T = T_{\text{F_in}})$$

$$h[1] = \text{enthalpy}(\text{CarbonDioxide}; P = P_{\text{sCO2}}; T = T_{\text{F}}[1])$$

"The last node"

$$q_{\text{gen_se}}[N_{\text{nodes}}] + (T_{\text{int_se}}[N_{\text{nodes}} - 1] - T_{\text{int_se}}[N_{\text{nodes}}]) / R_{\text{ax_EE}}[N_{\text{nodes}} - 1] = (T_{\text{int_se}}[N_{\text{nodes}}] - T_{\text{int_ch}}[N_{\text{nodes}}]) / R_{\text{ax_E_ch}}[N_{\text{nodes}}]$$

$$(T_{\text{int_se}}[N_{\text{nodes}}] - T_{\text{int_ch}}[N_{\text{nodes}}]) / R_{\text{ax_E_ch}}[N_{\text{nodes}}] + q_{\text{gen_ch}}[N_{\text{nodes}}] + (T_{\text{int_ch}}[N_{\text{nodes}} - 1] - T_{\text{int_ch}}[N_{\text{nodes}}]) / R_{\text{ax_ch}}[N_{\text{nodes}} - 1] = (T_{\text{int_ch}}[N_{\text{nodes}}] - T_{\text{W}}[N_{\text{nodes}}]) / R_{\text{ax_ch_w}}[N_{\text{nodes}}] + (T_{\text{int_ch}}[N_{\text{nodes}}] - T_{\text{int_sw}}[N_{\text{nodes}}]) / R_{\text{Ax_ch_sw}}[N_{\text{nodes}}]$$

$$q_{\text{gen_sw}}[N_{\text{nodes}}] + (T_{\text{int_ch}}[N_{\text{nodes}}] - T_{\text{int_sw}}[N_{\text{nodes}}]) / R_{\text{ax_ch_sw}}[N_{\text{nodes}}] + (T_{\text{int_sw}}[N_{\text{nodes}} - 1] - T_{\text{int_sw}}[N_{\text{nodes}}]) / R_{\text{ax_sw}}[N_{\text{nodes}} - 1] = 0$$

$$(T_{\text{int_ch}}[N_{\text{nodes}}] - T_{\text{W}}[N_{\text{nodes}}]) / R_{\text{ax_ch_w}}[N_{\text{nodes}}] = (T_{\text{W}}[N_{\text{nodes}}] - T_{\text{F}}[N_{\text{nodes}}]) / R_{\text{conv}}[N_{\text{nodes}}]$$

$$q_{\text{conv}}[N_{\text{nodes}}] = (T_{\text{W}}[N_{\text{nodes}}] - T_{\text{F}}[N_{\text{nodes}}]) / R_{\text{conv}}[N_{\text{nodes}}]$$

$$m_{\text{dot_chan}} * h[N_{\text{nodes}} - 1] + (T_{\text{W}}[N_{\text{nodes}}] - T_{\text{F}}[N_{\text{nodes}}]) / R_{\text{conv}}[N_{\text{nodes}}] = m_{\text{dot_chan}} * h[N_{\text{nodes}}]$$

$$h[N_{\text{nodes}}] = \text{enthalpy}(\text{CarbonDioxide}; P = P_{\text{sCO2}}; T = T_{\text{F}}[N_{\text{nodes}}])$$

"The internal nodes"

Duplicate i = 2; (N_nodes-1)

$$q_{\text{gen_se}}[i] + (T_{\text{int_SE}}[i - 1] - T_{\text{int_SE}}[i]) / R_{\text{ax_EE}}[i] = (T_{\text{int_se}}[i] - T_{\text{int_ch}}[i]) / R_{\text{ax_E_ch}}[i] + (T_{\text{int_SE}}[i] - T_{\text{int_SE}}[i + 1]) / R_{\text{ax_EE}}[i]$$

$$(T_{\text{int_se}}[i] - T_{\text{int_ch}}[i]) / R_{\text{ax_E_ch}}[i] + q_{\text{gen_ch}}[i] + (T_{\text{int_ch}}[i - 1] - T_{\text{int_ch}}[i]) / R_{\text{ax_ch}}[i] = (T_{\text{int_ch}}[i] - T_{\text{W}}[i]) / R_{\text{ax_ch_w}}[i] + (T_{\text{int_ch}}[i] - T_{\text{int_ch}}[i + 1]) / R_{\text{ax_ch}}[i] + (T_{\text{int_ch}}[i] - T_{\text{int_sw}}[i]) / R_{\text{Ax_ch_sw}}[i]$$

$$q_{\text{gen_sw}}[i] + (T_{\text{int_ch}}[i] - T_{\text{int_sw}}[i]) / R_{\text{Ax_ch_sw}}[i] + (T_{\text{int_sw}}[i - 1] - T_{\text{int_sw}}[i]) / R_{\text{ax_sw}}[i] = (T_{\text{int_sw}}[i] - T_{\text{int_sw}}[i + 1]) / R_{\text{ax_sw}}[i]$$

$$(T_{\text{int_ch}}[i] - T_{\text{W}}[i]) / R_{\text{ax_ch_w}}[i] = (T_{\text{W}}[i] - T_{\text{F}}[i]) / R_{\text{conv}}[i]$$

$$q_{\text{conv}}[i] = (T_{\text{W}}[i] - T_{\text{F}}[i]) / R_{\text{conv}}[i]$$

$$(m_dot_chan * h[i-1]) + (T_W[i] - T_F[i]) / R_conv[i] = (m_dot_chan * h[i])$$

$$h[i] = \text{enthalpy}(\text{CarbonDioxide}; P = P_sCO2; T = T_F[i])$$

End

Duplicate i=1; N_nodes

$$Q_duty_channel[i] = (T_int_ch[i] - T_W[i]) / R_ax_ch_w[i]$$

$$A_flux[i] = W_ch * L_CV[i]$$

$$q_flux[i] = q_duty_channel[i] / A_Flux[i]$$

End

"Check on the model"

$$Q_in_se = \text{sum}(q_gen_se[i]; i=1; N_nodes)$$

$$Q_in_sw = \text{sum}(q_gen_sw[i]; i=1; N_nodes)$$

$$Q_in_ch = \text{sum}(q_gen_ch[i]; i=1; N_nodes)$$

$$Q_total_in = Q_in_se + Q_in_sw + Q_in_ch$$

$$q_conv_tot = \text{sum}(q_conv[i]; i=1; N_nodes)$$

$$Q_out = m_dot_chan * (h[N_nodes] - h_in)$$

"Estimation of the frictional and acceleration pressure drops in the channel"

$$DP_total = \text{sum}(dp[i]; i=1; N_nodes)$$

"Total

frictional pressure drop inside a channel"

$$\rho_{in} = \text{density}(\text{CarbonDioxide}; P = P_sCO2; T = T_F_in)$$

"Density of

carbon dioxide at the test section inlet"

$$V_in = m_dot_chan / (\rho_{in} * A_cross_flow)$$

"Velocity at

the inlet"

$$\Delta acc[1] = \rho_{bulk}[1] * V_channel[1]^2 - \rho_{in} * V_in^2$$

$$\Delta Acc[1] = \rho_{in}[1] * V_channel[1]^2 - \rho_{in} * V_in^2$$

Duplicate i=2; N_nodes

$$\Delta Acc[i] = \rho_{bulk}[i] * V_channel[i]^2 - \rho_{bulk}[i-1] * V_channel[i-1]^2$$

End

"Flow acceleration parameter -- Bankston 1970 "

Duplicate i=1; N_nodes-1

$$K[i] = (\nu_{acc}[i] / V_channel[i]^2) * ((V_channel[i+1] - V_channel[i]) / L_CV[i])$$

$$\{Acc_st[i] = K[i] / St[i]\}$$

End

Duplicate i=1; N_nodes

$$\Delta acc_m[i] = \Delta Acc[i] / L_CV[i]$$

$$\Delta acc_patel[i] = -\nu_{acc}[i] / (\rho_{wall}[i] * u_{friction}[i]^3) * (dp_dx[i] + \Delta acc_m[i])$$

$$\Delta acc_tot[i] = dp[i] + \Delta acc_m[i]$$

End

"Data for analysis"

$$h_conv_mean = \text{average}(h_conv[1..40])$$

$$h_conv_max = \text{max}(h_conv[1..40])$$

$$Bo_max = \text{max}(Bo_pet[1..40])$$

$$Bo_min = \text{min}(Bo_pet[1..40])$$

$$K_v_max = \text{max}(K_v[1..40])$$

$$K_v_min = \text{min}(K_v[1..40])$$

$$T_W_max = \text{max}(T_W[1..40])$$

$$T_W_mean = \text{average}(T_W[1..40])$$

$$q_flux_mean = \text{average}(q_flux[1..40])$$